

$$\sin^6 x + \cos^6 x > \frac{5}{8}$$